



University of  
Zurich<sup>UZH</sup>

**ETH** zürich

Institute of Informatics – Institute of Neuroinformatics



ROBOTICS &  
PERCEPTION  
GROUP

# Lecture 10

# Multiple View Geometry 4

Davide Scaramuzza

<http://rpg.ifi.uzh.ch/>

# This afternoon: Intermediate VO Integration

19.09.2019	Lecture 01 - Introduction to Computer Vision and Visual Odometry	Davide Scaramuzza
26.09.2019	Lecture 02 - Image Formation 1: perspective projection and camera models Exercise 01 - Augmented reality wireframe cube	Davide Scaramuzza Daniel & Mathias Gehrig
03.10.2019	Lecture 03 - Image Formation 2: camera calibration algorithms Exercise 02 - PnP problem	Davide Scaramuzza Daniel & Mathias Gehrig
10.10.2019	Lecture 04 - Filtering & Edge detection	Davide Scaramuzza
17.10.2019	Lecture 05 - Point Feature Detectors, Part 1 Exercise 03 - Harris detector + descriptor + matching	Davide Scaramuzza Daniel & Mathias Gehrig
24.10.2019	Lecture 06 - Point Feature Detectors, Part 2 Exercise 04 - SIFT detector + descriptor + matching	Davide Scaramuzza Daniel & Mathias Gehrig
31.10.2019	Lecture 07 - Multiple-view geometry Exercise 05 - Stereo vision: rectification, epipolar matching, disparity, triangulation	Davide Scaramuzza Daniel & Mathias Gehrig
07.11.2019	Lecture 08 - Multiple-view geometry 2 Exercise 06 - Eight-Point Algorithm	<span style="color: red;">Antonio Loquercio</span> Daniel & Mathias Gehrig
14.11.2019	Lecture 09 - Multiple-view geometry 3 (Part 1)	Davide Scaramuzza
21.11.2019	Lecture 10 - Multiple-view geometry 3 (Part 2) Exercise session: Intermediate VO Integration	Davide Scaramuzza Daniel & Mathias Gehrig
28.11.2019	Lecture 11 - Optical Flow and Tracking (Lucas-Kanade) Exercise 08 - Lucas-Kanade tracker	Davide Scaramuzza Daniel & Mathias Gehrig
05.12.2019	Lecture 12 - Place recognition and 3D Reconstruction Exercise session: Deep Learning Tutorial	Davide Scaramuzza Daniel & Mathias Gehrig
12.12.2019	Lecture 13 - Visual inertial fusion Exercise 09 - Bundle Adjustment	Davide Scaramuzza Daniel & Mathias Gehrig
19.12.2019	Lecture 14 - Event based vision After the lecture, we will Scaramuzza's lab. Departure from lecture room at 12:00 via tram 10. Exercise session: Final VO Integration	Davide Scaramuzza Daniel & Mathias Gehrig

How can we evaluate VO/SLAM algorithms?

This problem is known as “Benchmarking”

# Popular Datasets for VO/SLAM Benchmarking

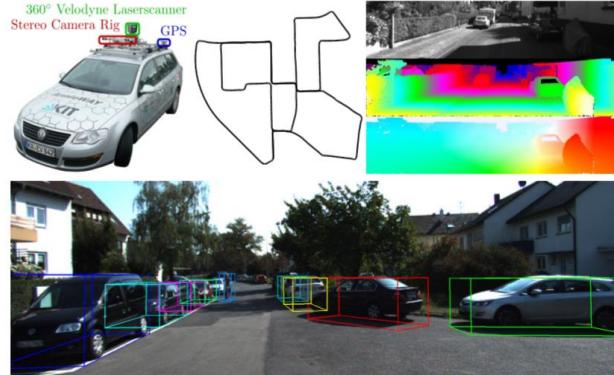
## Devon Island [Furgale'11]

Stereo + D-GPS + inclinometer + sun sensor



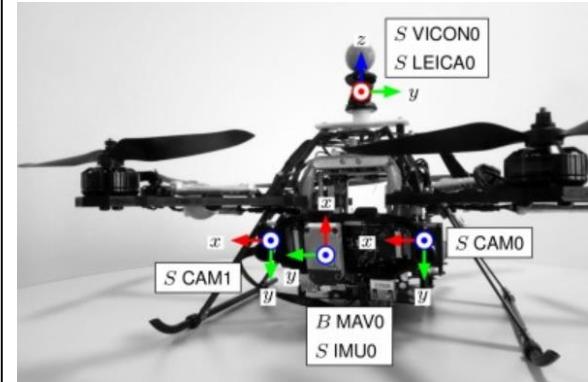
## KITTI [Geiger'12]

Automobile, Laser + stereo + GPS, multiple tasks



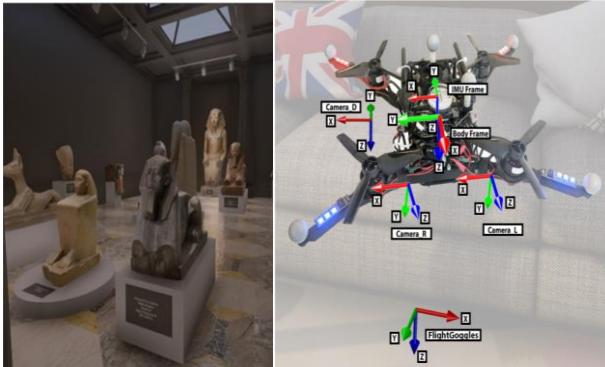
## EuRoC [Burri'16]

MAV with synchronized IMU and stereo



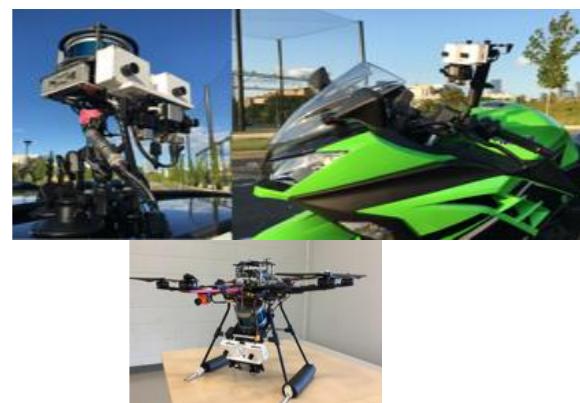
## Blackbird [Antonini'18]

MAV indoor aggressive flight with rendered images and real dynamics + IMU



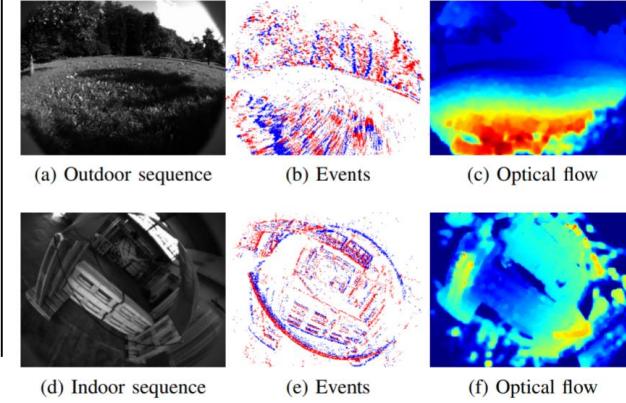
## MVSEC [Zhu'18]

Events, frames, lidar, GPS, IMU from cars, drones, and motorcycles

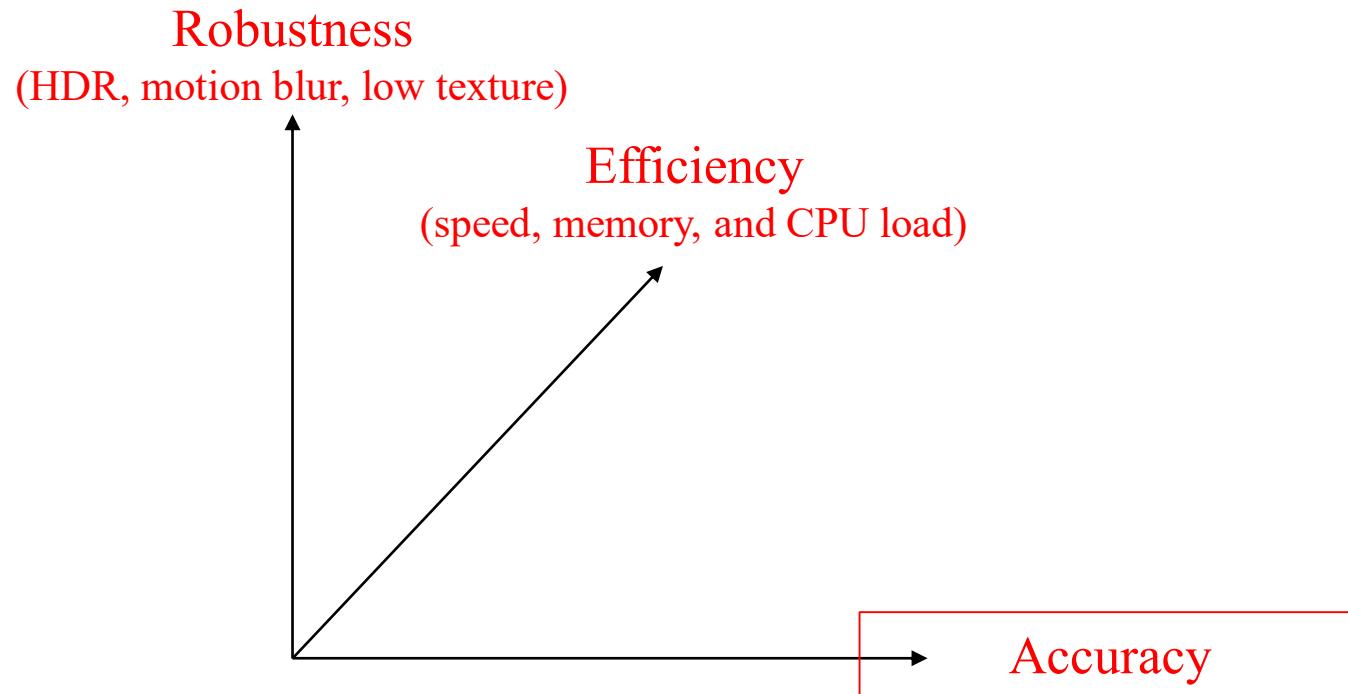


## UZH Drone Racing [Delmerico'19]

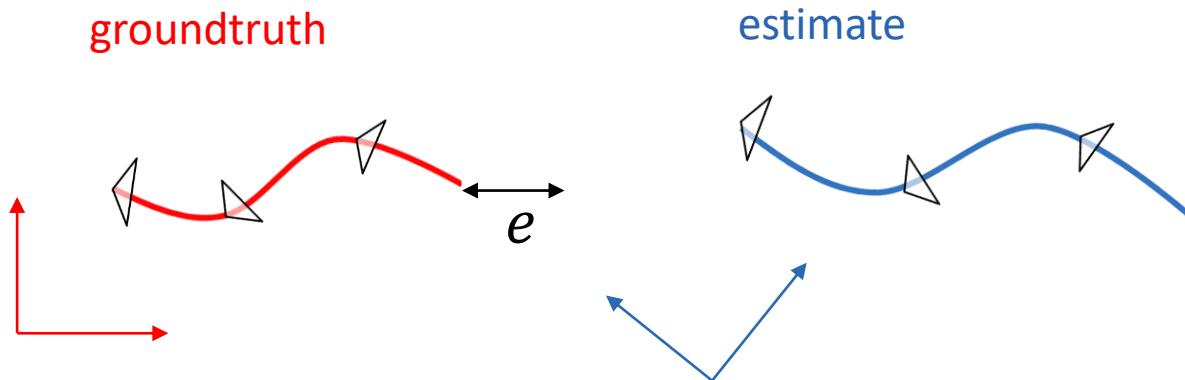
MAV aggressive flight, standard + event cameras, IMU, indoors and outdoors



# What metrics should be used?



# Evaluation is a non-trivial task...



## Direct difference?

- Different reference frame
- Different scale
- Different times stamps
- ...

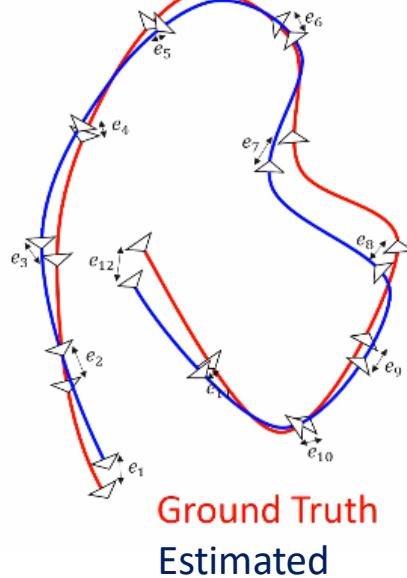
Maybe align the first poses and measure the **end-pose error**?

- **How many poses** should be used for the alignment?
- **Not robust:**
  - **Most VIOs are non-deterministic** (e.g., RANSAC, multithreading) → every time you run your VIO on the same dataset, you get different results
  - **Not meaningful:**
    - too sensitive to the trajectory shape
    - does not capture the error statistics

# Metric 1: Absolute Trajectory Error (ATE)

## Absolute Trajectory Error

RMSE of the aligned estimate and the groundtruth.



- ✓ Single number metric
- ✗ Many parameters to specify

## Step 1: Align the trajectory

$$\underset{R,T,s}{\operatorname{argmin}} \sum_{i=0}^N \|\hat{t}_i - sRt_i - T\|^2$$

Alignment parameters

groundtruth positions

estimated positions

## Step 2: Root mean squared errors between the aligned estimate and the groundtruth.

$$\sqrt{\frac{\sum_{i=1}^N \|\hat{t}_i - sRt_i - T\|^2}{N}}$$

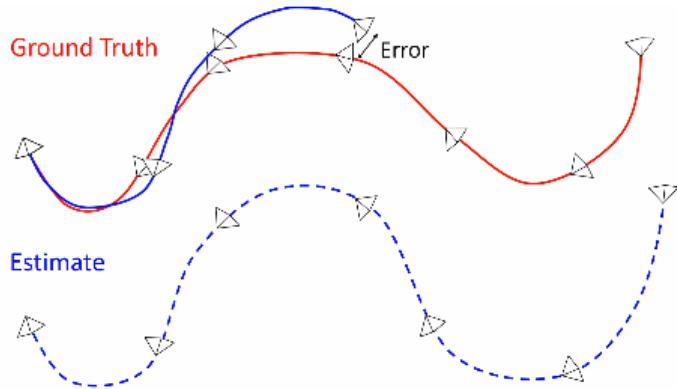
- Sturm et al., "A benchmark for the evaluation of RGB-D SLAM systems." IROS 2012.
- Zhang et al., "A tutorial on quantitative trajectory evaluation for visual (-inertial) odometry." IROS'18. [PDF](#)

# Metric 2: Relative Trajectory Error (RTE)

## Relative Error (Odometry Error)

Statistics of sub-trajectories of specified lengths.

- Calculate errors for all the subtrajectories of certain lengths.



- ✓ Informative statistics
- ✗ Complicated to compute and rank

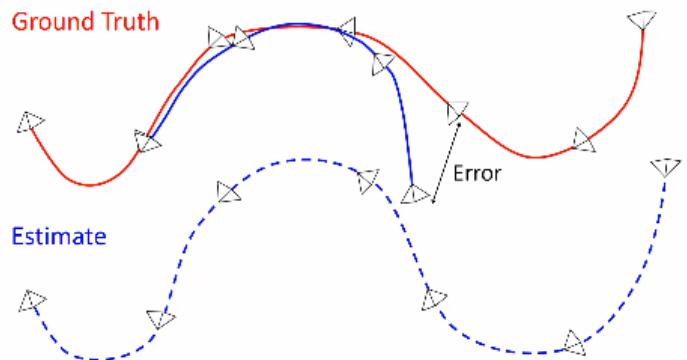
- Geiger et al. "Are we ready for autonomous driving? the KITTI vision benchmark suite." CVPR 2012.
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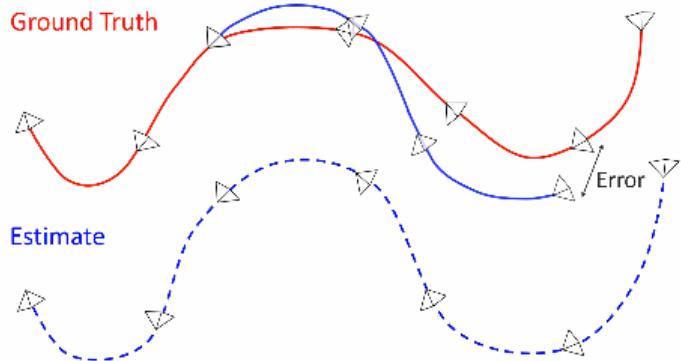
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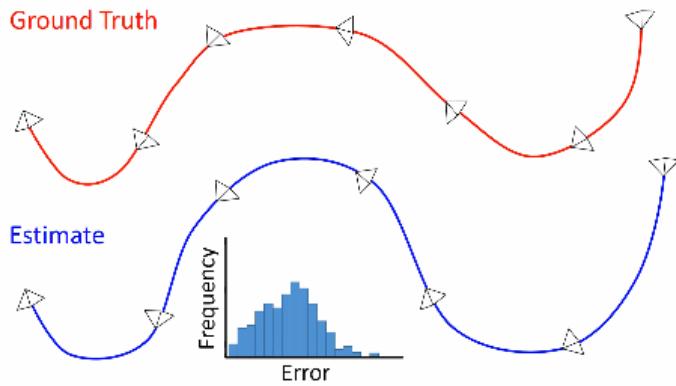
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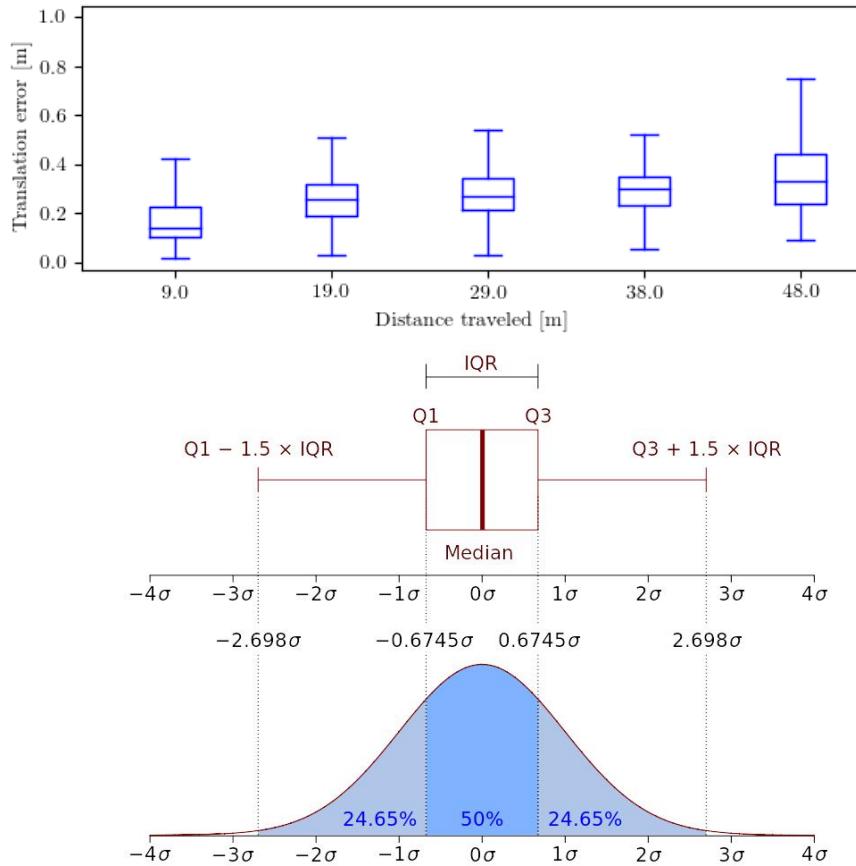
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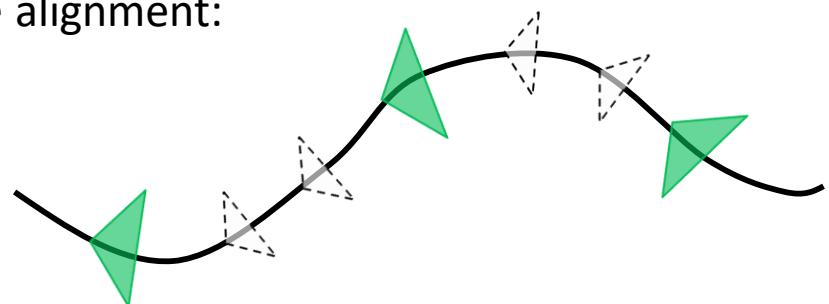
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# Trajectory Accuracy: Error Metrics

- Both ATE and RTE are widely used in practice, but:
  - **Many details** need to be specified which are **often omitted in papers**
    - **Number of poses** used for the alignment (also, **frames or keyframes?**)
    - **Type of transformation used** for the alignment:
      - **SE(3)** for stereo VO
      - **Sim(3)** for monocular VO
      - **4DOF** for VIO
    - **Sub-trajectory lengths** in RTE
      - White: **Normal frames** (used for **real time pose update**)
      - Green: **Keyframes** (usually updated **after BA**)



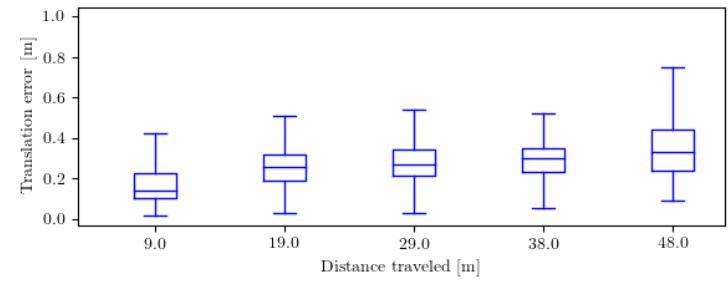
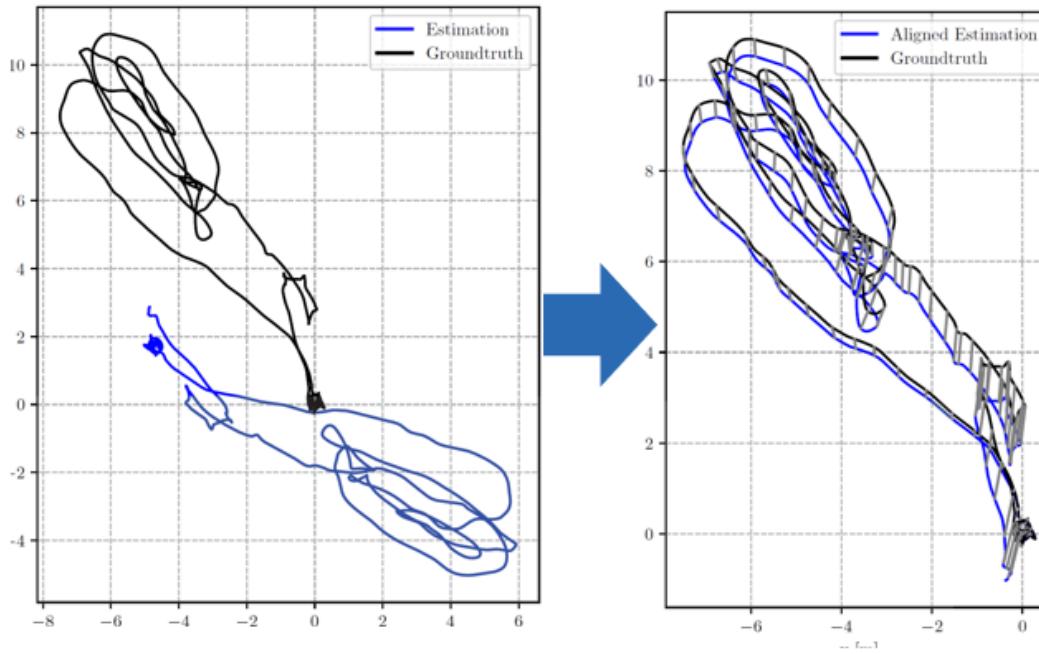
- Results are not directly comparable with different settings
  - **Report the evaluation settings** in detail.
  - Is there a publicly available evaluation tool to facilitate reproducible evaluation? Yes: **Trajectory Evaluation Toolbox**

# Trajectory Evaluation Toolbox

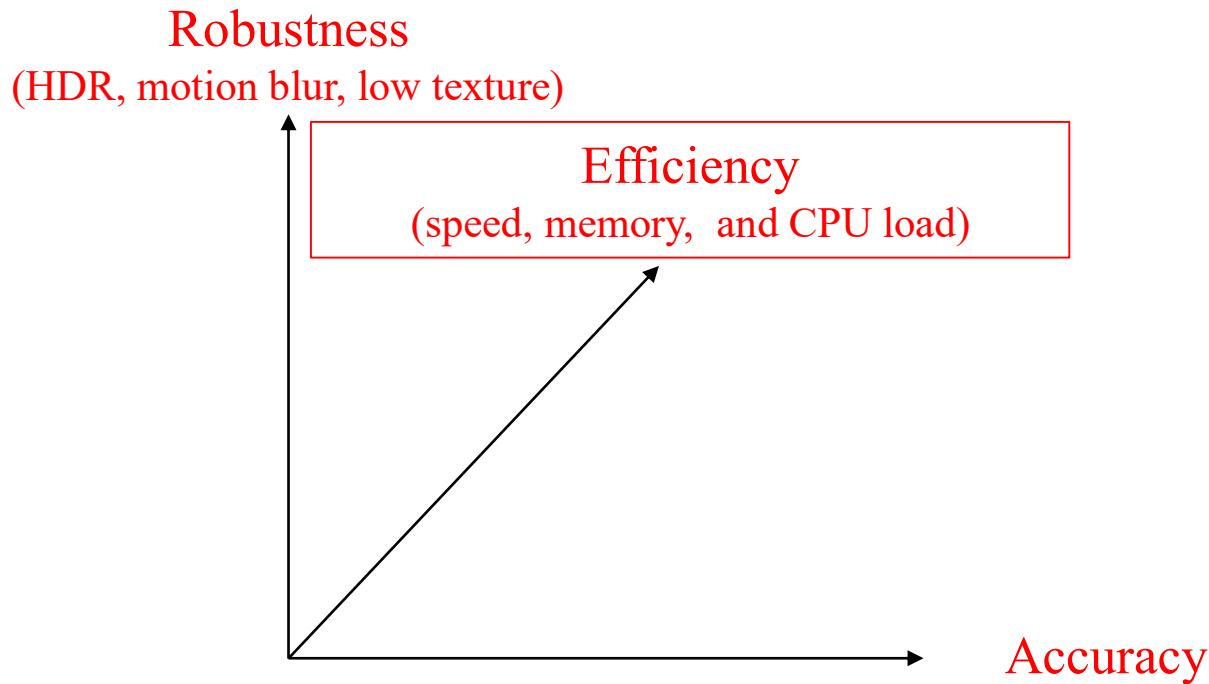
## ➤ Designed to make trajectory evaluation easy!

- Implements **different alignment methods** depending on the sensing modalities: **SE(3)** for stereo, **sim(3)** for monocular, **4DOF** for VIO.
- Implements **Absolute Trajectory Error** and **Relative Error**.
- Automated evaluation of different algorithms on multiple datasets (for N runs).

➤ Code: [https://github.com/uzh-rpg/rpg\\_trajectory\\_evaluation](https://github.com/uzh-rpg/rpg_trajectory_evaluation) [Zhang, IROS'18]



# What metrics should be used?



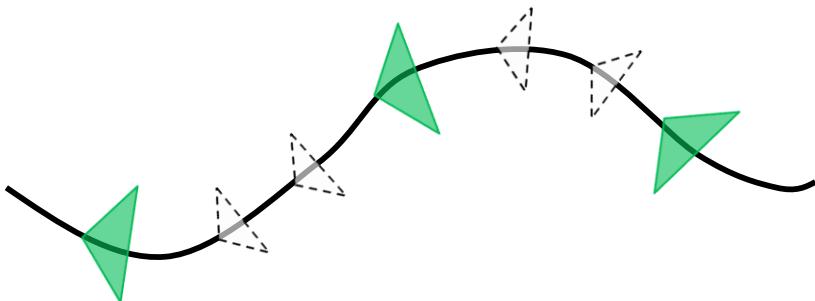
# Benchmarking Efficiency

## ➤ Different computational resources

- Memory
- CPU load
- Processing time

Depends not only on algorithm design, but also implementation, platforms, etc.

## ➤ There are **different definitions of processing time** in SLAM systems.



- White: Normal frames (used for real time pose update)
- Green: Keyframes (usually updated after BA)

- **Processing time for real-time pose:**  
 $t_{pose\ output} - t_{image\ arrival}$
- **Processing time for asynchronously executed threads** (e.g., bundle adjustment)
  - .....

# Case study: VIO for Flying Robots [ICRA'18]

- Algorithms: **MSCKF**, **OKVIS**, **ROVIO**, **VINS-Mono**, **SVO+MSF**, **SVO+GTSAM**, VINS-Mono w/ and w/o loop closure
- Hardware: consider the limitation of flying robots



Intel NUC



Odroid XU4



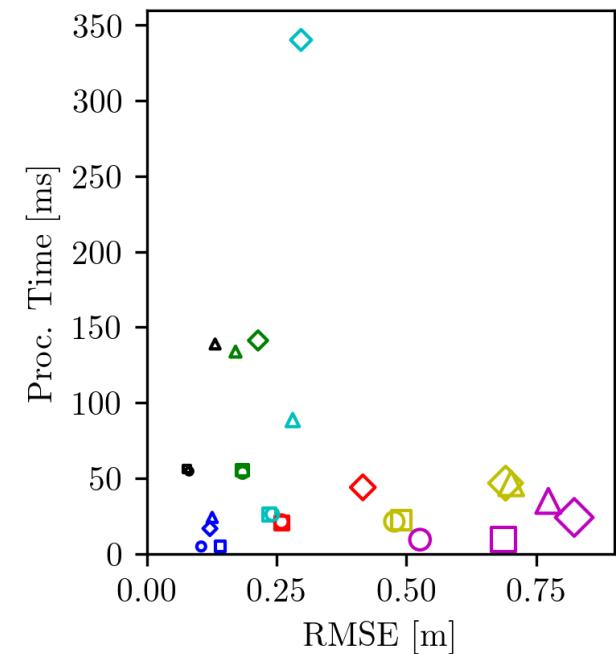
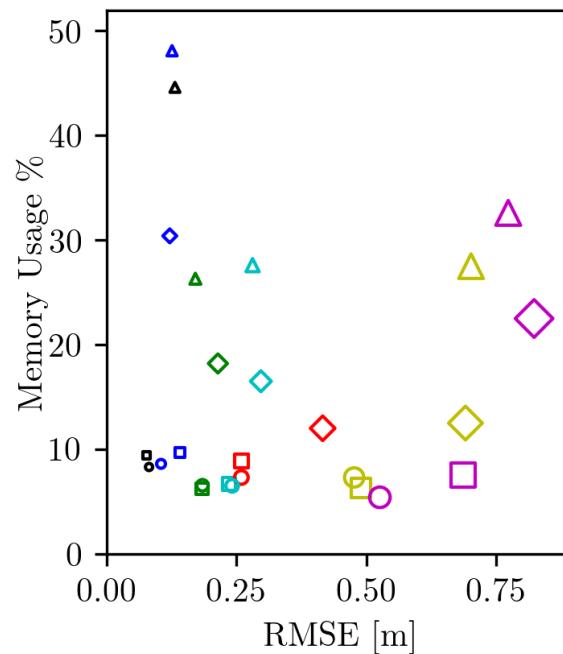
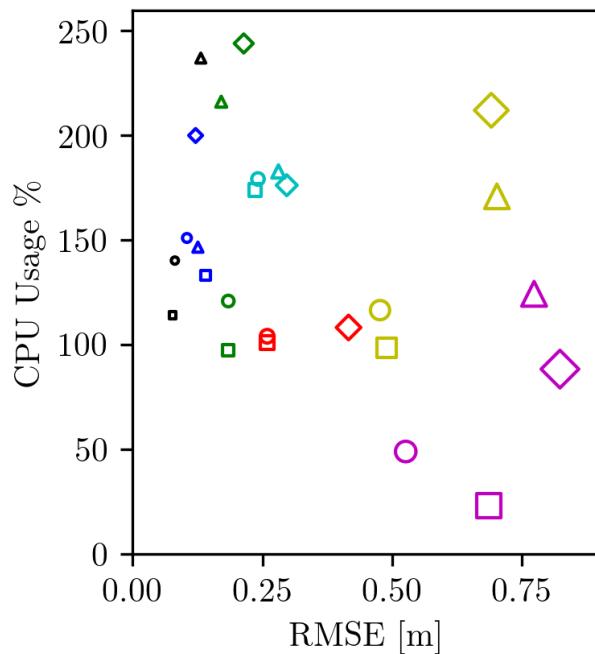
Up Board



Intel Lenovo  
W540 i7laptop

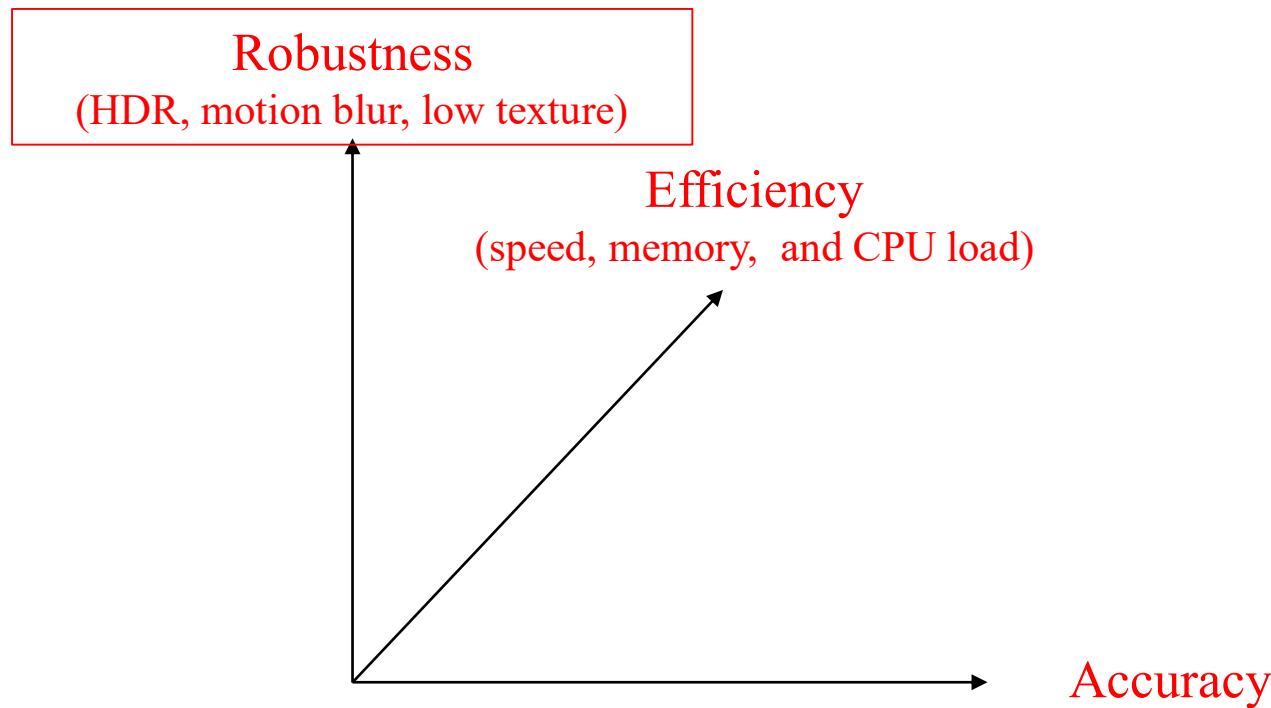
- Evaluation
  - **Absolute Trajectory Error (ATE)**— RMSE after sim(3) trajectory alignment (7DoF)
  - **Relative Trajectory Error (RTE)**— Error distribution of the subtrajectories
  - **CPU usage** – total load of CPU
  - **Memory usage** – total percentage of available RAM
  - **Time per frame** – from input until pose is updated

# Case study: VIO for Flying Robots [ICRA'18]



**No free lunch:** more computation → better accuracy

# What metrics should be used?



# Robustness is the greatest challenge for SLAM today!

How to cope & quantify robustness to:

- Low texture
- High Dynamic Range (HDR) scenes
- Motion blur
- Dynamically changing environments
- Algorithmic randomness

**How can we quantify the robustness of algorithms to such situations?**

**High Dynamic Range**



**Motion blur**

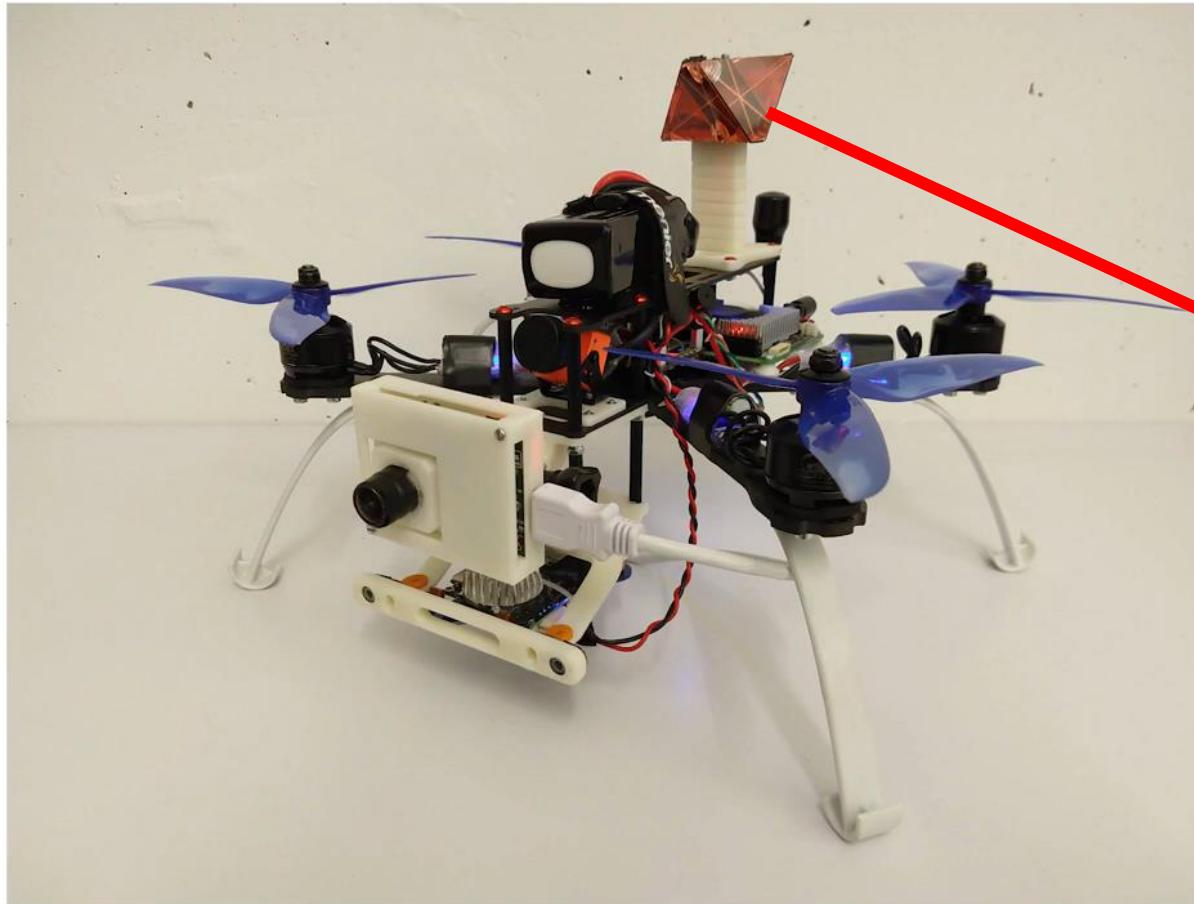


**Latency**



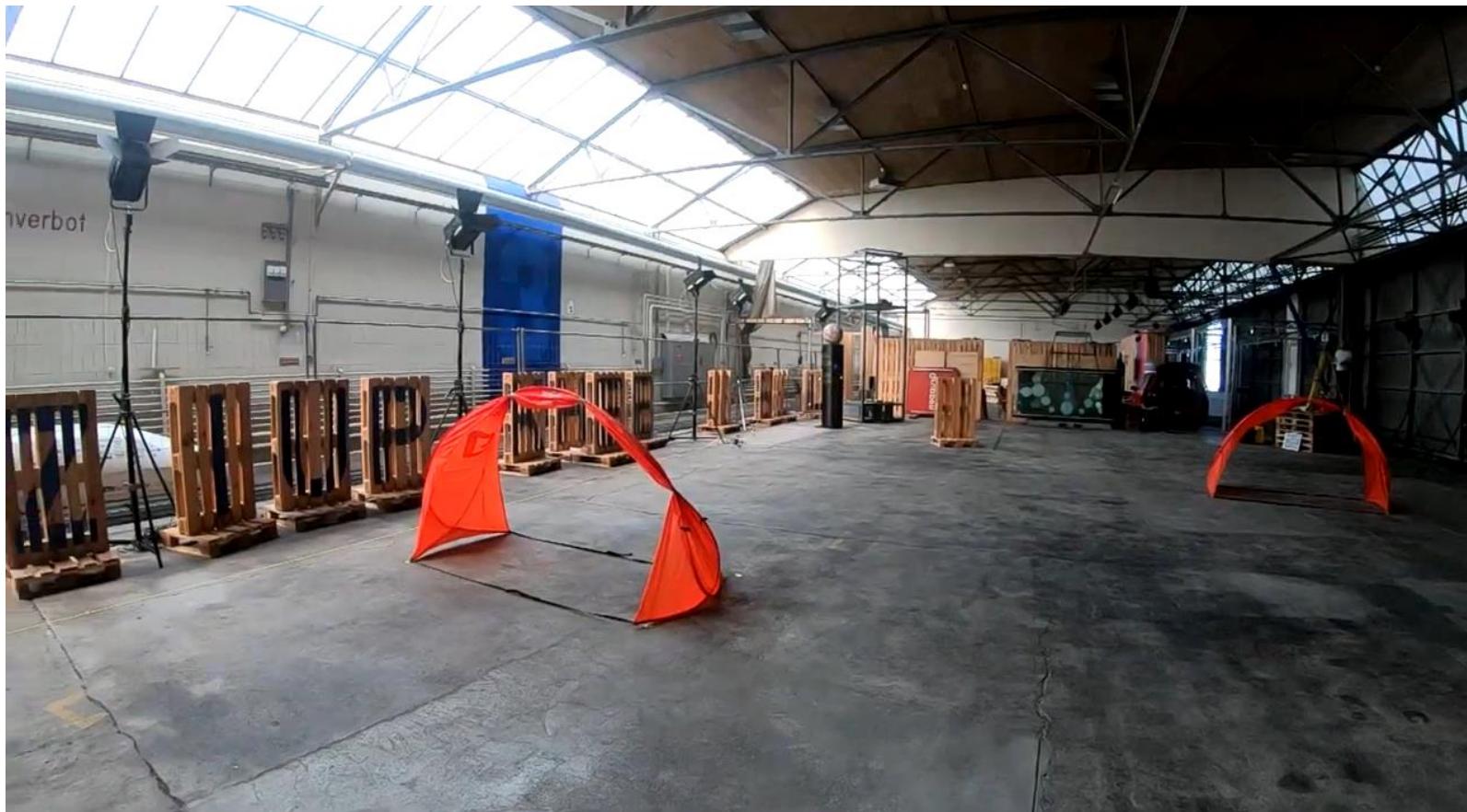
# UZH-FPV Drone Racing Dataset

Contains data recorded by a drone flying up to over 20m/s indoors and outdoors flown by a professional pilot. Contains frames, events, IMU, and Ground Truth from a Robotic Total Station: <http://rpg.ifi.uzh.ch/uzh-fpv.html>



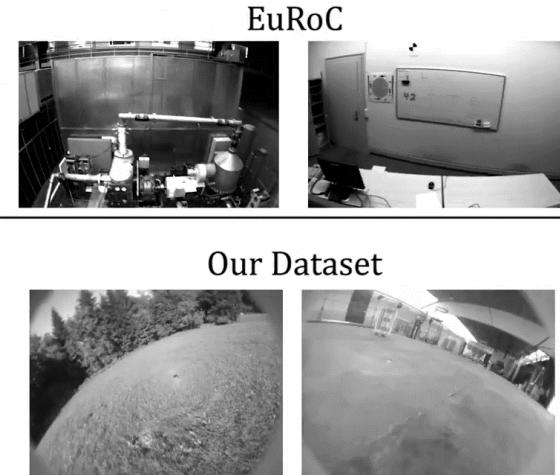
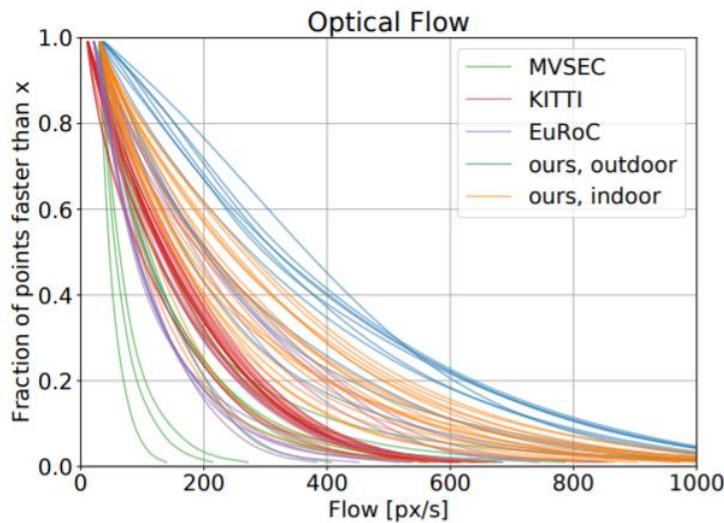
# UZH-FPV Drone Racing Dataset

- Recorded with a drone flown by a **professional pilot up to over 20m/s**
- Contains **images, events, IMU, and ground truth from a robotic total station:**  
<http://rpg.ifi.uzh.ch/uzh-fpv.html>



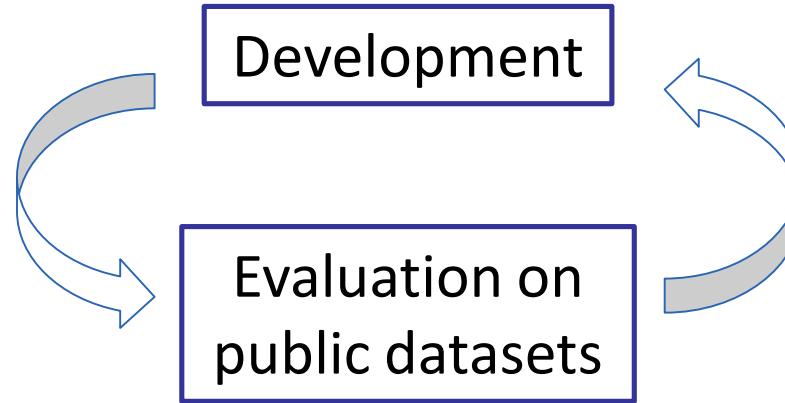
# Robustness to high speed motion

Can be quantified in terms of “optical flow” (see Lecture 10 for def. of optical flow)



# Dataset Bias

Typical workflow of developing VO/VIO/SLAM algorithms:



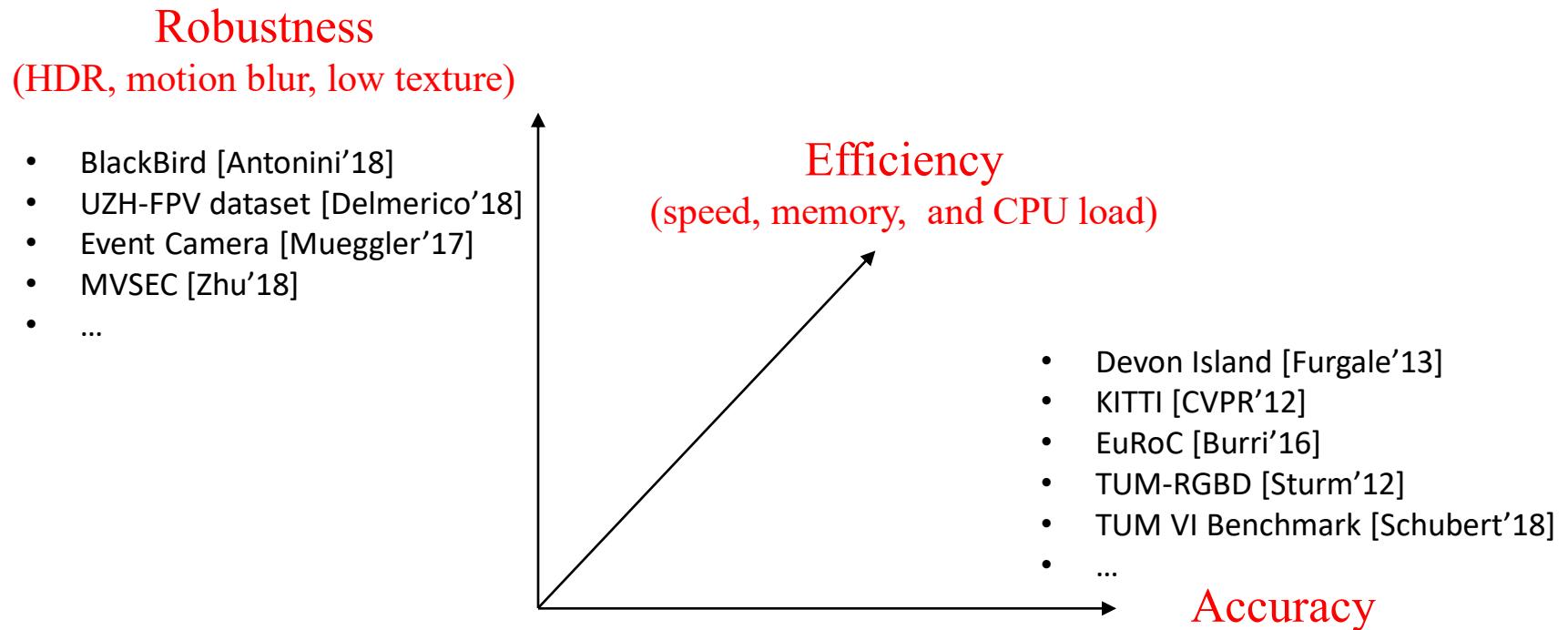
**As a community, we are overfitting the public dataset.**

Potential problems:

- **Generalizability:** Performance on one does not guarantee to generalize to others
  - E.g., KITTI → low frame rate, not friendly for direct methods
- **Old datasets (e.g., KITTI) are already saturated:**
  - It becomes more and more difficult to tell whether we are making real progress or just overfitting the datasets.
  - E.g., **does 1 or 2 cm improvement in RMSE over a 100 meter trajectory really mean something?**

# Dataset Bias

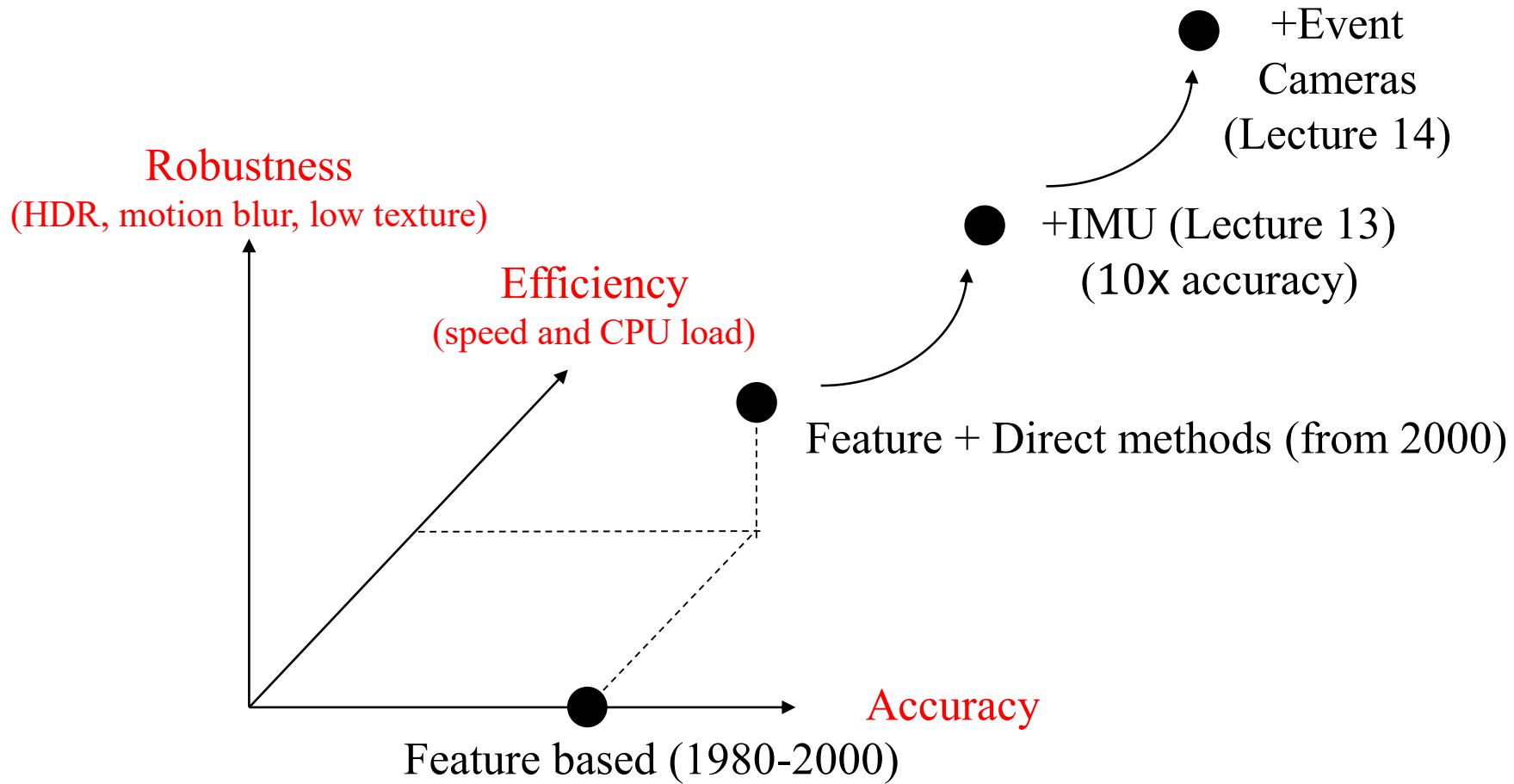
We need more datasets to evaluate the performance of SLAM algorithms along different axes



## Realistic simulators:

- AirSim
- FlightGoggles [Guerra'19]
- ESIM [Rebecq'18]
- .....

# Overview of the last 30 years of Visual Inertial Odometry & SLAM

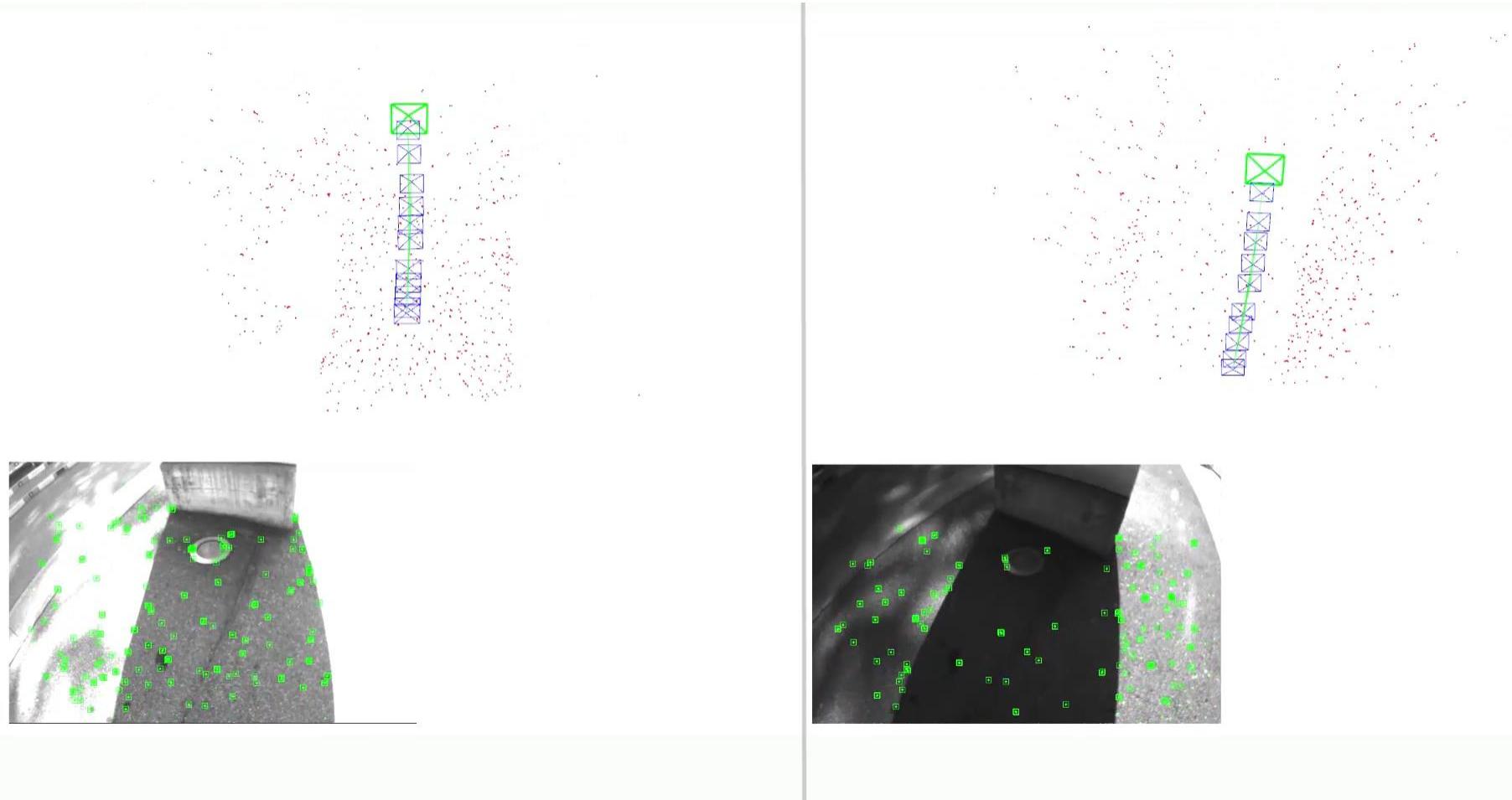


# Open Research Opportunities

# Actively Control Camera Exposure Time to achieve Robustness to High Dynamic Range (HDR) scenes

ORB-SLAM with  
Standard Built-in Auto-Exposure

ORB-SLAM with  
Our Active Exposure Control



**2 x**

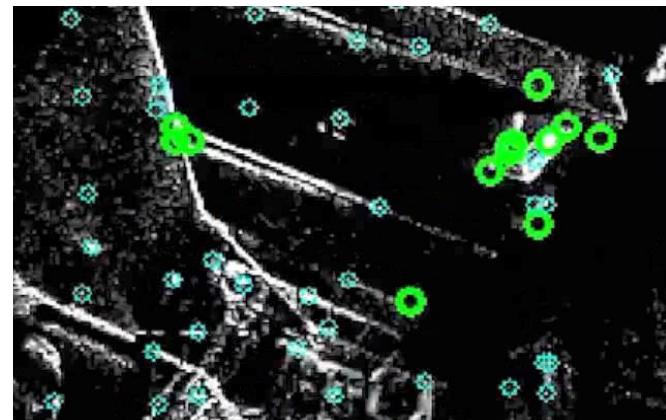
# “UltimateSLAM”: Frames + Events + IMU (Lecture 14)

85% accuracy gain over standard visual-inertial SLAM in HDR and high speed scenes

Standard camera

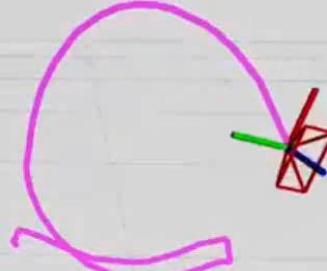


Event camera

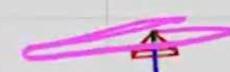


Estimated trajectory

Front view



Top view



# Understanding Check

Are you able to answer the following questions:

- How do we benchmark VO/SLAM algorithms?
- Along which axes can we evaluate them?
- Benchmarking accuracy: Can we use the end pose error? What are ATE and RTE?
- How can we quantify Efficiency? And Robustness?
- What are open research opportunities?